



**NATIONAL  
SENIOR CERTIFICATE/  
*NASIONALE  
SENIOR SERTIFIKAAT***

**GRADE/GRAAD 12**

**SEPTEMBER 2022**

**MATHEMATICS P2/WISKUNDE V2  
MARKING GUIDELINE/*NASIENRIGLYN***

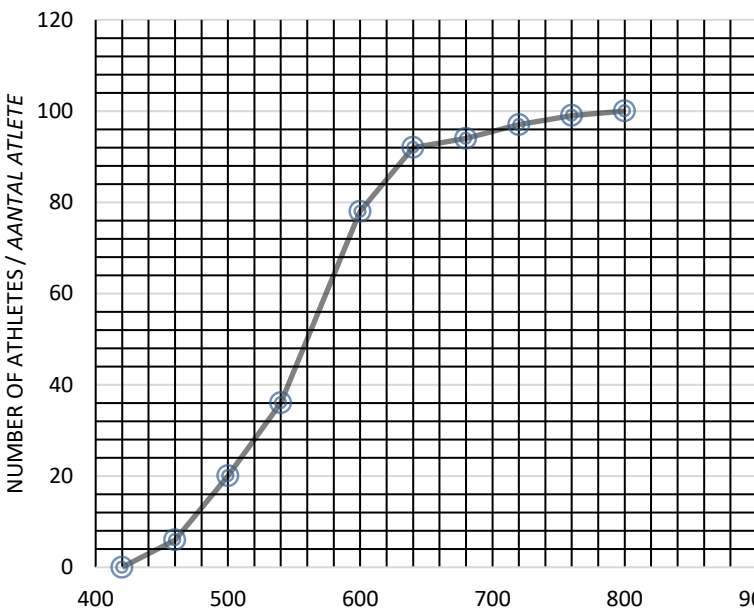
**MARKS/PUNTE: 150**

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This marking guideline consists of 16 pages./  
*Hierdie nasienriglyn bestaan uit 16 bladsye.*

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## QUESTION 1/VRAAG 1

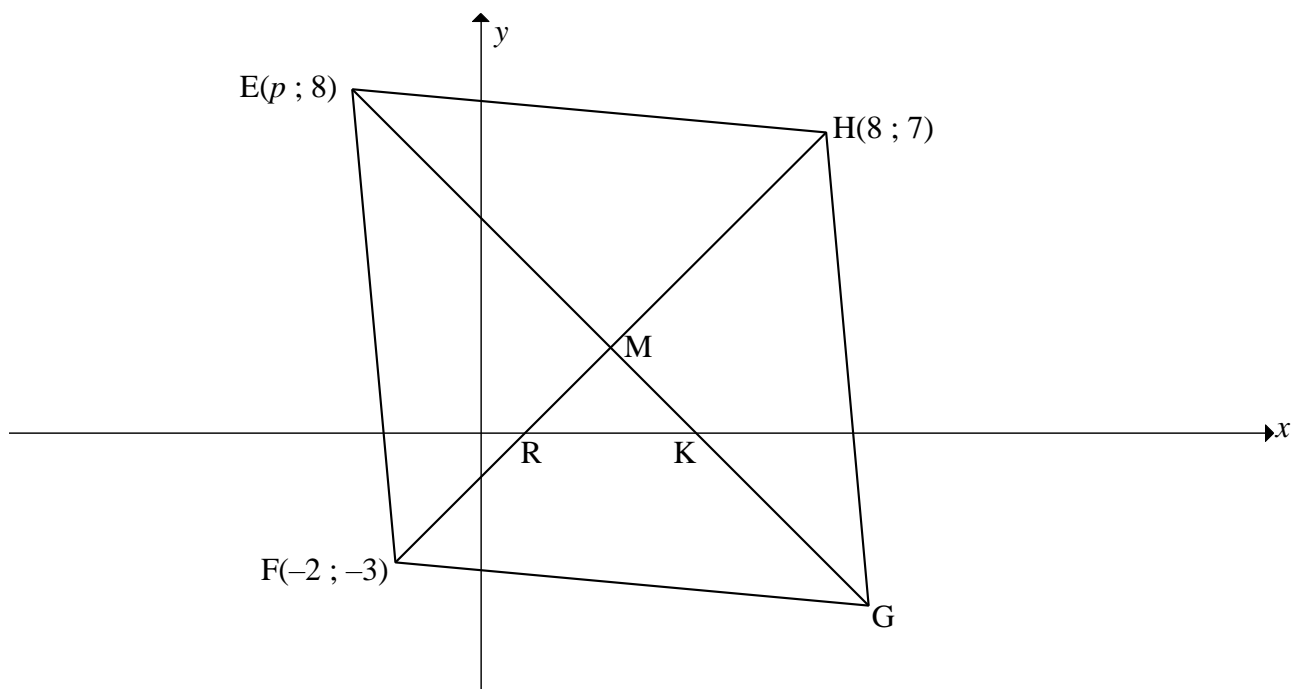
1.1	<table><tr><th>Distance of Jumps <i>Afstand van Spronge</i> (in cm)</th><th>Number of athletes <i>Aantal atlete</i></th><th>CF <i>KF</i></th></tr><tr><td><math>420 &lt; d \leq 460</math></td><td>6</td><td>6</td></tr><tr><td><math>460 &lt; d \leq 500</math></td><td>14</td><td>20</td></tr><tr><td><math>500 &lt; d \leq 540</math></td><td>16</td><td>36</td></tr><tr><td><math>540 &lt; d \leq 580</math></td><td>42</td><td>78</td></tr><tr><td><math>580 &lt; d \leq 620</math></td><td>14</td><td>92</td></tr><tr><td><math>620 &lt; d \leq 660</math></td><td>2</td><td>94</td></tr><tr><td><math>660 &lt; d \leq 700</math></td><td>3</td><td>97</td></tr><tr><td><math>700 &lt; d \leq 740</math></td><td>2</td><td>99</td></tr><tr><td><math>740 &lt; d \leq 780</math></td><td>1</td><td>100</td></tr></table>	Distance of Jumps <i>Afstand van Spronge</i> (in cm)	Number of athletes <i>Aantal atlete</i>	CF <i>KF</i>	$420 < d \leq 460$	6	6	$460 < d \leq 500$	14	20	$500 < d \leq 540$	16	36	$540 < d \leq 580$	42	78	$580 < d \leq 620$	14	92	$620 < d \leq 660$	2	94	$660 < d \leq 700$	3	97	$700 < d \leq 740$	2	99	$740 < d \leq 780$	1	100	<div>✓ for cf [6 to 92] <i>vir kf [6 tot 92]</i></div> <div>✓ for cf [94 to 100] <i>vir kf [94 tot 100]</i></div>	(2)
Distance of Jumps <i>Afstand van Spronge</i> (in cm)	Number of athletes <i>Aantal atlete</i>	CF <i>KF</i>																															
$420 < d \leq 460$	6	6																															
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1.2	<div><div>LONG JUMPERS' BEST JUMPS <i>VERSPRINGERS SE BESTE SPRONGE</i></div></div>	<div>✓ anchor point <i>ankerpunt</i></div> <div>✓ upper limits <i>boonste limiete</i></div> <div>✓ sf /</div> <div>✓ smooth shape <i>egalige vorm</i></div>	(4)																														
1.3	The median jump is 553. Accept between (551 – 555) <i>Die mediaan sprong is 553. Aanvaar tussen (551 – 555)</i>	<div>✓✓ for answer <i>vir antwoord</i></div>	(2)																														
1.4	Number jumped over 560 cm = 100 – 57 = 43 athletes Therefore, it is 43% of the athletes. <i>Aantal wat oor 560 cm gespring het = 100 – 57 = 43 atlete</i> <i>Dit is daarom 43% van die atlete.</i>	<div>✓ for subtraction <i>vir aftrekking</i></div> <div>✓ for the answer <i>vir die antwoord</i></div>	(2)																														
[10]																																	

## QUESTION 2/VRAAG 2

Long jumper / Verspringer	1	2	3	4	5	6
x: Hours practised / Ure geoefen	4,5	2	3,5	4	8	3
y: Distance jumped / Afstand gespring (cm)	650	420	580	490	780	525

2.1	$a = 336,699$ $b = 56,992$ $\hat{y} = 336,699 + 56,992x$	✓ for/vir a ✓ for/vir b ✓ for/vir $a + bx$	(3)
2.2	$\hat{y} = 336,699 + 56,992(5.4) = 644,46$ cm	✓ for substitution vir vervanging ✓ for the answer vir die antwoord	(2)
2.3	The more they practiced, the further they jumped. Strong positive correlation. <i>Hoe meer hulle geoefen het, hoe verder het hulle gespring.</i> <i>Sterk positiewe korrelasie.</i>	✓✓ for the answer vir die antwoord	(2)
2.4.1	The mean will decrease by 13 cm. <i>Die gemiddelde sal met 13 cm verminder.</i>	✓ for the answer vir die antwoord	(1)
2.4.2	The range will remain the same / No influence on range. <i>Die omvang sal dieselfde bly / Geen invloed op die omvang.</i>	✓ for the answer vir die antwoord	(1)
2.4.3	The standard deviation remains the same. <i>Die standaardafwyking bly dieselfde.</i>	✓ for the answer vir die antwoord	(1)
			[10]

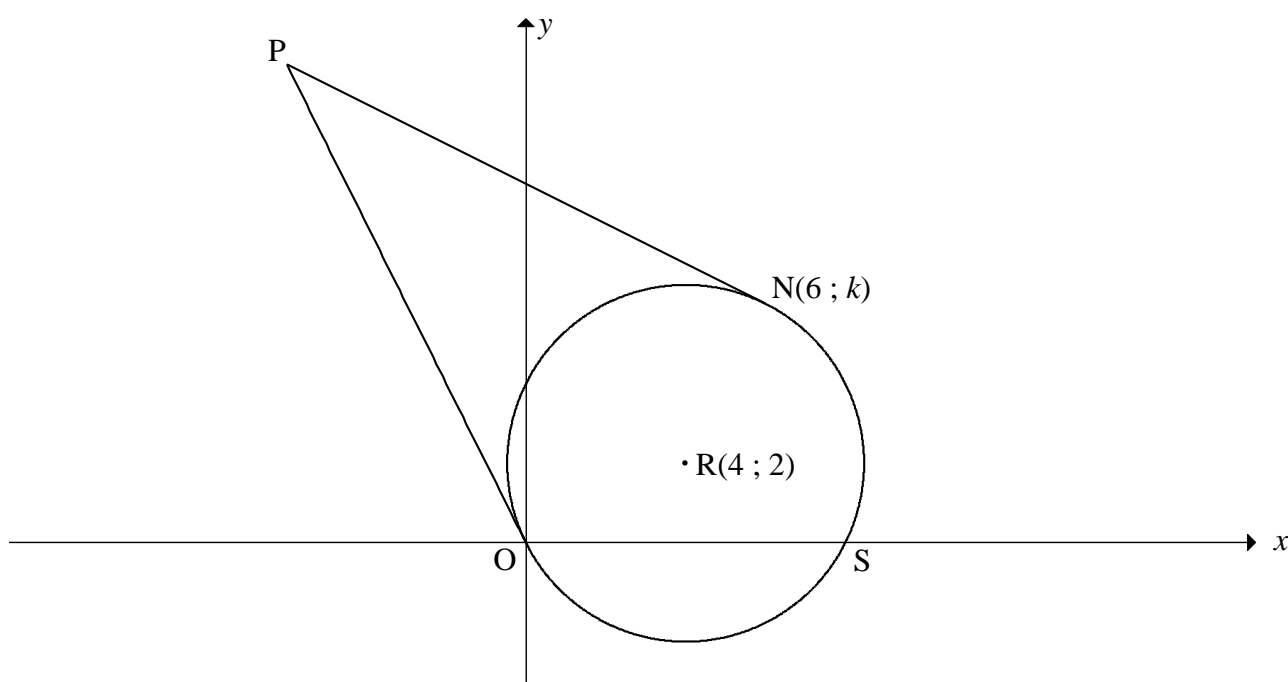
## QUESTION 3/VRAAG 3



3.1.1	M (3; 2)	✓ for/vir $x$ ✓ for/vir $y$	(2)
3.1.2	$m_{FH} = \frac{7 - (-3)}{8 - (-2)} = 1$	✓ for subst. / vir vervanging ✓ for answer / vir antwoord	(2)
3.1.3	$m_{EG} = -1$ (diagonals bisect at $90^\circ$ ) (hoeklyne halveer loodreg/by $90^\circ$ ) $\tan \widehat{MKX} = -1$ $\widehat{MKX} = 135^\circ$ $\therefore \widehat{MKR} = 45^\circ$	✓ S  ✓ S ✓ $\widehat{MKX} = 135^\circ$ ✓ for answer / vir antwoord	(4)

3.2	<p>FE = EH (sides of a rhombus = ) (syé van 'n rombus = )</p> $FE^2 = EH^2$ $(p+2)^2 + (8+3)^2 = (p-8)^2 + (8-7)^2$ $p^2 + 4p + 4 + 121 = p^2 - 16p + 64 + 1$ $20p = -120$ $p = -3$ <p style="text-align: center;"><b>OR/OF</b></p> <p>E(p; 8) and Midpoint of HF / en Middelpunt van HF = (3; 2)</p> $m_{FH} = 1$ <p>gradient from E to midpoint of FH / gradiënt vanaf E na middelpunt van FH</p> $= \frac{8-2}{p-3} = \frac{6}{p-3}$ <p>FH is perpendicular to EG / FH is loodreg op EG</p> $\therefore \frac{6}{p-3} \times 1 = -1$ $\therefore p = -3$	<p>✓ for equating / gelykstel <math>FE^2 = EH^2</math></p> <p>✓ for squaring / kwadrering</p> <p>✓ for simplification vir vereenvoudiging</p> <p>✓ for the answer vir die antwoord</p> <p style="text-align: center;"><b>OR/OF</b></p> <p>✓ for gradient of E to FH vir gradiënt van E na FH</p> <p>✓ statement / stelling</p> <p>✓ for the product vir die produk</p> <p>✓ for the answer vir die antwoord</p>	(4)
3.3	G(9; - 4)	✓ for/vir x    ✓ for/vir y	(2)
3.4	<p>M(3 ;2)</p> <p>N(-9 ;2)</p> <p>MN = 12 units/eenhede</p>	<p>✓ for coordinates of N vir die koördinate van N</p> <p>✓✓ for answer / vir antwoord</p>	(3)
			<b>[17]</b>

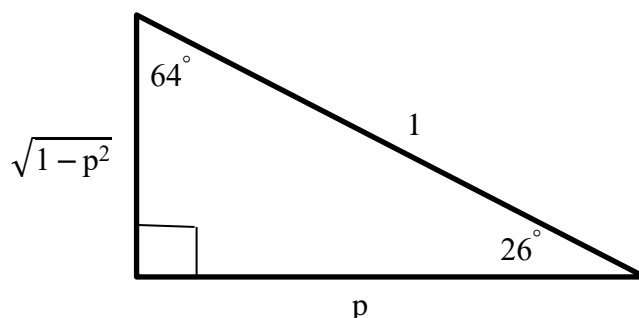
## QUESTION/VRAAG 4



4.1	$r^2 = (4-0)^2 + (2-0)^2$ $r^2 = 20$ $\therefore (x-4)^2 + (y-2)^2 = 20$	✓ substitution / <i>vervang</i> ✓ for/vir $r^2$  ✓ for the equation/vir <i>die vergelyking</i>	(3)
4.2	$(6-4)^2 + (k-2)^2 = 20$ $(k-2)^2 = 16$ $k-2 = \pm 4$ $k = 6$ or/of $k = -2$ $k = 6$  <p style="text-align: center;"><b>OR/OF</b></p> Sub: $N(6; y)$ into the equation of the circle. <i>Verv. <math>N(6; y)</math> in die vergelyking van die sirkel.</i> $(6-4)^2 + (y-2)^2 = 20$ $4 + y^2 - 4y + 4 - 20 = 0$ $y^2 - 4y - 12 = 0$ $(y-6)(y+2) = 0$ $y = 6$ or/of $y = -2$ $\therefore y = 6$	✓ substitution of / <i>vervang</i> van N ✓ simplification / <i>vereenvoudiging</i> ✓ both answers for k / <i>beide antwoorde vir k</i> ✓ selection of $k = 6$ <i>keuse van <math>k = 6</math></i> <p style="text-align: center;"><b>OR/OF</b></p> ✓ for substitution / <i>vir vervang</i>  ✓ for standard form / <i>vir standaardvorm</i> ✓ for the factors / <i>vir die faktore</i>  ✓ for the answer / <i>vir die antwoord</i>	(4)

4.3	$m_{RN} = \frac{6-2}{6-4} = 2$ $m_{NP} = -\frac{1}{2}$ <p>Equation of NP / <i>Vergelyking van NP</i>:</p> $y - 6 = -\frac{1}{2}(x - 6)$ $y = -\frac{1}{2}x + 9$	✓ for gradient of RN <i>vir gradiënt van RN</i> ✓ for gradient of NP <i>vir gradiënt van NP</i> ✓ for substitution of N <i>vir vervanging van N</i>  ✓ for/vir $c = 9$  ✓ for answer / <i>vir antwoord</i>	(5)
4.4.1	$-2x = -\frac{1}{2}x + 9$ $-\frac{3}{2}x = 9$ $-3x = 18$ $\therefore x = -6 \text{ and/en } y = 12$ $\therefore P(-6; 12)$	✓ for equating / <i>vir gelykstelling</i>  ✓ for the simplification <i>vir die vereenvoudiging</i>  ✓ for the answer / <i>vir die antwoord</i>	(3)
4.4.2	$RO = RN = \sqrt{4^2 + 2^2} = 2\sqrt{5} \text{ (radii/radiusse)}$ $PO = PN = \sqrt{(-6)^2 + 12^2} = 6\sqrt{5} \text{ (tangents from same pt)}$ <p style="text-align: center;"><i>(raaklyne vanaf dieselfde punt)</i></p> $\therefore \text{Perimeter of / Omtrek van PNRO} = 2(2\sqrt{5}) + 2(6\sqrt{5})$ $= 16\sqrt{5} \text{ or/of } 35,78 \text{ units/eenhede}$	✓ use of distance formula <i>gebruik van afstand formule</i> ✓ for RO / RN answer <i>vir RO / RN antwoord</i> ✓ for PO / PN answer <i>vir PO / PN antwoord</i>  ✓ for final answer <i>vir finale antwoord</i>	(4)
4.5	$S(8 ; 0)$ $T(12 ; -2)$	✓✓ coordinates of S <i>koördinate van S</i> ✓✓ coordinates of T <i>koördinate van T</i>	(4)
			[23]

## QUESTION 5/VRAAG 5

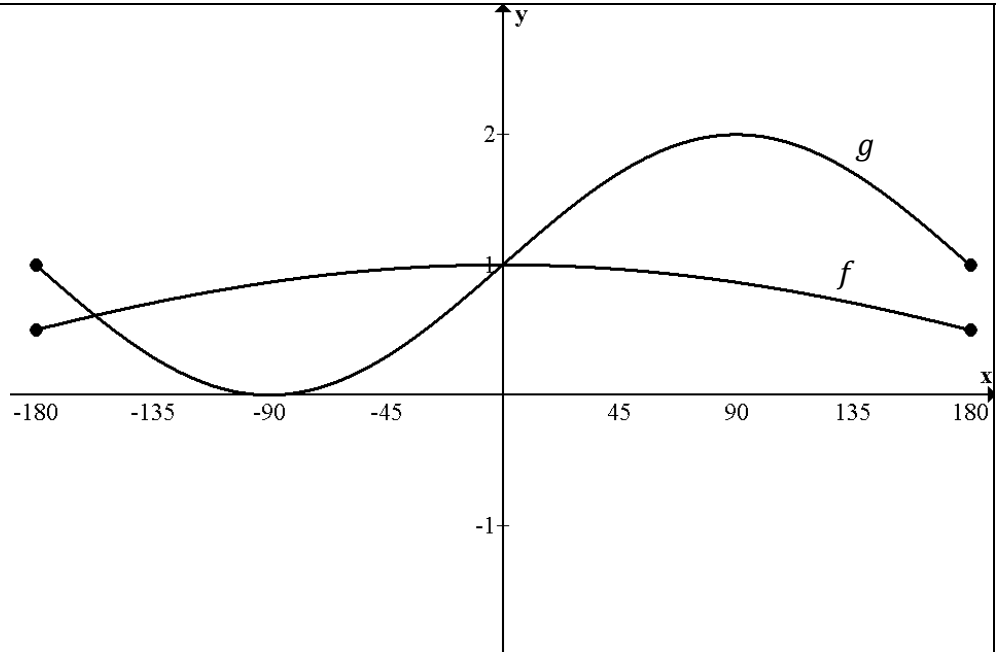


5.1.1	$\sin 26^\circ = \frac{\sqrt{1-p^2}}{1}$	✓✓ for the answer <i>vir die antwoord</i>	(2)
5.1.2	$\tan 154^\circ$ $= -\tan 26^\circ$ $= -\frac{\sqrt{1-p^2}}{p}$	✓✓ for the reduction <i>vir die reduksie</i> ✓ for the answer <i>vir die antwoord</i>	(3)
5.1.3	$\sin 13^\circ \cdot \cos 13^\circ$ $\sin 26^\circ = 2 \sin 13^\circ \cdot \cos 13^\circ$ $\sin 13^\circ \cdot \cos 13^\circ = \frac{\sin 26^\circ}{2}$ $\sin 13^\circ \cdot \cos 13^\circ = \frac{\sqrt{1-p^2}}{2}$	✓ for the reduction <i>vir die reduksie</i> ✓ for the answer <i>vir die antwoord</i>	(2)
5.2.1	$\frac{\cos(-\theta) \cdot \tan(180^\circ + \theta)}{2 \cos(90^\circ + \theta)}$ $= \frac{\cos \theta \cdot \tan \theta}{-2 \sin \theta}$ $= \frac{\cos \theta \cdot \frac{\sin \theta}{\cos \theta}}{-2 \sin \theta}$ $= -\frac{1}{2}$	✓ $\cos \theta$ ✓ $\tan \theta$ ✓ $-2 \sin \theta$ ✓ $\frac{\sin \theta}{\cos \theta}$ ✓ for the answer <i>vir die antwoord</i>	(5)
5.2.2	$1 + 2 \cos 105^\circ \sin 15^\circ$ $= 1 + 2 \cos 75^\circ \sin 15^\circ$ $= 1 + 2 \sin 15^\circ \sin 15^\circ$ $= 1 - \sin 30^\circ$ $= 1 - \frac{1}{2}$ $= \frac{1}{2}$	✓ for reduction of $\cos 105^\circ$ <i>vir reduksie van <math>\cos 105^\circ</math></i> ✓ for reduction of $\cos 75^\circ$ <i>vir reduksie van <math>\cos 75^\circ</math></i> ✓ for $\sin 30^\circ$ <i>vir <math>\sin 30^\circ</math></i> ✓ for the answer <i>vir die antwoord</i>	(4)

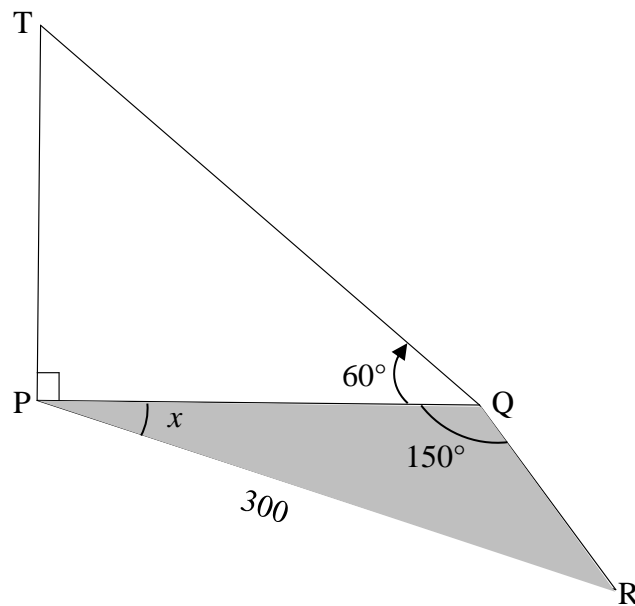


5.3.1	$\frac{1 - \cos 2x - \sin x}{\sin 2x - \cos x} = \tan x$ <p>LHS:</p> $\frac{1 - (1 - 2\sin^2 x) - \sin x}{2\sin x \cos x - \cos x}$ $= \frac{2\sin^2 x - \sin x}{2\sin x \cos x - \cos x}$ $= \frac{\sin x(2\sin x - 1)}{\cos x(2\sin x - 1)}$ $= \tan x = \text{RHS}$	<ul style="list-style-type: none"> <li>✓ expansion of <math>\cos 2x</math> <i>uitbreiding van <math>\cos 2x</math></i></li> <li>✓ expansion of <math>\sin 2x</math> <i>uitbreiding van <math>\sin 2x</math></i></li> <li>✓ for the simplification <i>vir die vereenvoudiging</i></li> <li>✓ taking out HCF <i>uithaal van GGD</i></li> </ul>	(4)
5.3.2	$\sin 2x = \cos x$  $x = -90^\circ ; 30^\circ ; 90^\circ \text{ and/en } 150^\circ$	<ul style="list-style-type: none"> <li>✓ for/vir <math>\sin 2x = \cos x</math></li> <li>✓ for any 2 answers <i>vir enige 2 antwoorde</i></li> <li>✓ for any other 2 answers <i>vir enige 2 antwoorde</i></li> </ul>	(3)
5.4	$\sin^2 x + 2\sin x \cos x = 3\cos^2 x$ $\sin^2 x + 2\sin x \cos x - 3\cos^2 x = 0$ Divide every term by/ <i>Deel elke term deur</i> $\cos^2 x$ $\tan^2 x + 2\tan x - 3 = 0$ $(\tan + 3)(\tan - 1) = 0$ $\tan x = -3 \text{ or/of } \tan x = 1$ $x = 108,43^\circ + 180^\circ.k \text{ or/of } x = 45^\circ + 180^\circ.k$ where/ <i>waar</i> $k \in \mathbb{Z}$  <p style="text-align: center;"><b>OR/OF</b></p> $\sin^2 x + 2\sin x \cos x = 3\cos^2 x$ $\sin^2 x + 2\sin x \cos x - 3\cos^2 x = 0$ $(\sin x + 3\cos x)(\sin x - \cos x) = 0$ $\sin x = -3\cos x \text{ or/of } \sin x = \cos x$ $\tan x = -3 \text{ or/of } \tan x = 1$ $x = 108,43^\circ + 180^\circ.k$ or/ <i>of</i> $x = 45^\circ + 180^\circ.k$ where/ <i>waar</i> , $k \in \mathbb{Z}$	<ul style="list-style-type: none"> <li>✓ for standard form <i>vir standaardvorm</i></li> <li>✓ for dividing by <math>\cos^2 x</math> <i>vir deling deur <math>\cos^2 x</math></i></li> <li>✓ for the factors <i>vir die faktore</i></li> <li>✓ for values of <math>\tan x</math> <i>vir waardes van <math>\tan x</math></i></li> <li>✓✓ for the answers <i>vir die antwoorde</i></li> </ul> <ul style="list-style-type: none"> <li>✓ for standard form <i>vir standaardvorm</i></li> <li>✓ for the factors <i>vir die faktore</i></li> <li>✓ for isolating <math>\sin x</math> <i>vir isolering van <math>\sin x</math></i></li> <li>✓ for values of <math>\tan x</math> <i>vir waardes van <math>\tan x</math></i></li> <li>✓✓ for the answers <i>vir die antwoorde</i></li> </ul>	(7)
			[30]

## QUESTION 6/VRAAG 6

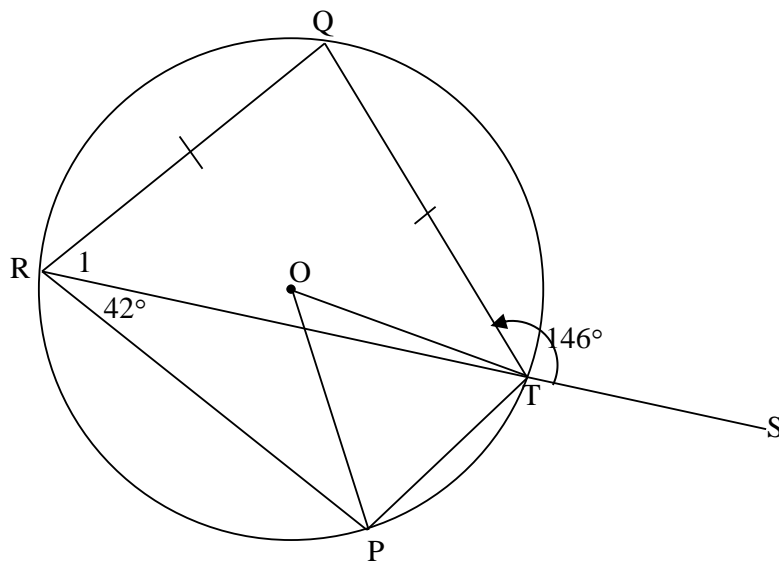
6.1			✓ shape vorm  ✓ start / end points begin / eind punte  ✓ TP at / DP by 90°	(3)
6.2.1	Period / Periode = 180°		✓ answer	(1)
6.2.2	$-3 \leq y \leq -1$  <b>OR/OF</b>  $y \in [-3 ; -1]$	✓ for/vir -3 and/en -1 ✓ for the answer in correct notation vir die antwoord in korrekte notasie		(2)
6.3	$h(x) = -\sin x - 1$ Maximum distance/Maksimum afstand = 2 units/eenhede	✓ for/vir $h(x)$ ✓ answer / antwoord		(2)
6.4	$f(x) \cdot g'(x) > 0$  $-90^\circ < x < 90^\circ$	✓✓ answer / antwoord		(2)
6.5	Graph shifted 1 unit down and 15° to the right. Grafiek het 1 eenheid af en 15° na regs geskuif.	✓ for 1 unit down / vir 1 eenheid af ✓ for 15° to the right / vir 15° na regs		(2)
				<b>[12]</b>

## QUESTION 7/VRAAG 7



7.1	$\hat{R}(30^\circ - x)$	✓ for answer / <i>vir antwoord</i>	(1)
7.2	$\frac{PQ}{\sin(30^\circ - x)} = \frac{300}{\sin 150^\circ}$ $\frac{PQ}{\sin(30^\circ - x)} = 600$ $PQ = 600 \sin(30^\circ - x)$	✓ for sine-rule <i>vir sinusreël</i>  ✓ for/vir 600  ✓ for the answer <i>vir die antwoord</i>	(3)
7.3	$\tan 60^\circ = \frac{TP}{PQ}$ $TP = PQ \tan 60^\circ$ $TP = \sqrt{3} \cdot 600 \sin(30^\circ - x)$ $TP = \sqrt{3} \cdot 600 \cdot (\sin 30^\circ \cos x - \cos 30^\circ \sin x)$ $TP = \sqrt{3} \cdot 600 \left( \frac{1}{2} \cos x - \frac{\sqrt{3}}{2} \sin x \right)$ $TP = \sqrt{3} \cdot 300 (\cos x - \sin x)$	✓ for/vir $\tan 60^\circ$  ✓ for/vir $\sqrt{3} \cdot 600 \sin(30^\circ - x)$  ✓ for expansion <i>vir uitbreiding</i> ✓ for taking out common factor / <i>vir uithaal van</i> <i>gemene faktor</i>	(4)
			[8]

## QUESTION 8/VRAAG 8

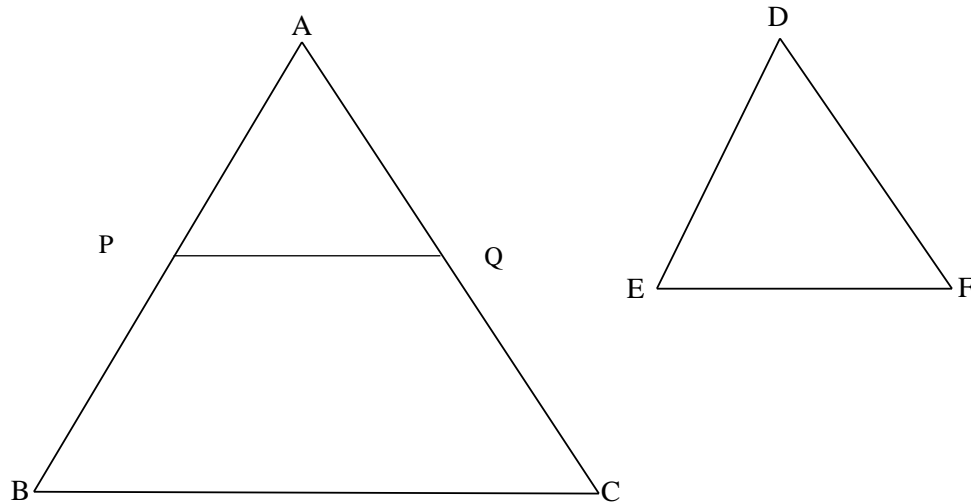


8.1	$\widehat{POT} = 84^\circ$ ( $\angle$ at centre ) / ( <i>Middelpunts <math>\angle</math></i> )	✓ S ✓ R	(2)
8.2	$\widehat{QTR} = 34^\circ$ ( $\angle$ s on a straight line ) ( <i><math>\angle</math> e op 'n reguitlyn</i> )	✓ S and/en R	
	$\widehat{R_1} = 34^\circ$ ( $\angle$ s opp. = sides ) / ( <i><math>\angle</math> e teenoor = sye</i> )	✓ S and/en R	(2)
8.3	$\widehat{RQT} = 112^\circ$ $\widehat{RPT} = 68^\circ$ ( opp. $\angle$ s of cq ) / ( <i>teenoorst. <math>\angle</math> e van kv</i> )	✓ S and/en R ✓ S ✓ R	(3)
			[7]



9.2.3	<p>In <math>\triangle MEC</math>:</p> <p><math>CE \parallel DB</math> (proven / bewys)</p> <p><math>\frac{ME}{MB} = \frac{MC}{MD}</math> (prop. int. Thm, <math>CE \parallel DB</math>)</p> <p>(eweredigheid st, <math>CE \parallel DB</math>)</p> <p><math>\therefore \frac{ME}{MC} = \frac{MB}{MD}</math></p> <p><math>\therefore ME \times MD = MC \times MB</math></p>	<p>✓ S and/en R</p> <p>✓ S</p>	(2)
			<b>[12]</b>

## QUESTION 10/VRAAG 10



10.1	<p>Construction: Mark off, on AB and AC, P and Q respectively such that <math>AP = DE</math> and <math>AQ = DF</math>.  <i>Konstruksie: Merk P en Q onderskeidelik op AB en AC af sodat <math>AP = DE</math> en <math>AQ = DF</math>.</i></p> <p>In <math>\triangle PAQ</math> and/en <math>\triangle EDF</math>:</p> <p>(1) <math>PA = ED</math> (construction / <i>konstruksie</i>)  (2) <math>\hat{A} = \hat{D}</math> (given / <i>gegee</i>)  (3) <math>QA = FD</math> (construction / <i>konstruksie</i>)  <math>\therefore \triangle PAQ \equiv \triangle EDF</math> (SAS)  <math>\therefore \hat{APQ} = \hat{E}</math> (congruency / <i>kongruensie</i>)  But/<i>Maar</i> <math>\hat{B} = \hat{E}</math> (given/<i>gegee</i>)  <math>\therefore \hat{APQ} = \hat{E}</math>  <math>\therefore PQ \parallel BC</math> (corresponding <math>\angle</math>s = / <i>ooreenkomstige. <math>\angle e =</math></i>)  <math>\therefore \frac{AP}{AB} = \frac{AQ}{AC}</math> (prop. int. thm / <i>eweredigheid stelling</i>)  But/<i>Maar</i> :  <math>AP = DE</math> and/en <math>AQ = DF</math> (construction/<i>konstruksie</i>)  <math>\therefore \frac{DE}{AB} = \frac{DF}{AC}</math></p>	<p>✓ construction  <i>konstruksie</i></p> <p>✓ S and/en R</p> <p>✓ S  ✓ S ✓ R  ✓ S</p>	(6)
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