



**education**

**MPUMALANGA PROVINCE  
REPUBLIC OF SOUTH AFRICA**

**NATIONAL  
SENIOR CERTIFICATE**

**GRADE 12**

**MATHEMATICS P2**

**JUNE 2023**

**MARKING GUIDELINE**

**MARKS: 150 marks**

**This question paper consists of 13 pages and an information sheet.**



**NOTE:**

1. If a candidate answered a question TWICE, mark only the FIRST attempt.
2. If a candidate crossed out an answer and did not redo it, mark the crossed-out answer.
3. Consistent accuracy applies to ALL aspects of the marking memorandum.
4. Assuming values/answers in order to solve a problem is unacceptable.



**LET WEL:**

5. As 'n kandidaat 'n vraag TWEE keer beantwoord het, sien slegs die EERSTE poging na.
6. As 'n kandidaat 'n antwoord deurgehaal en nie oorgedoen het nie, sien die deurgehaalde antwoord na.
7. Volgehoue akkuraatheid is op ALLE aspekte van die memorandum van toepassing.
8. Dit is onaanvaarbaar om waardes/antwoorde te veronderstel om 'n probleem op te los.
9. Write neatly and legibly.

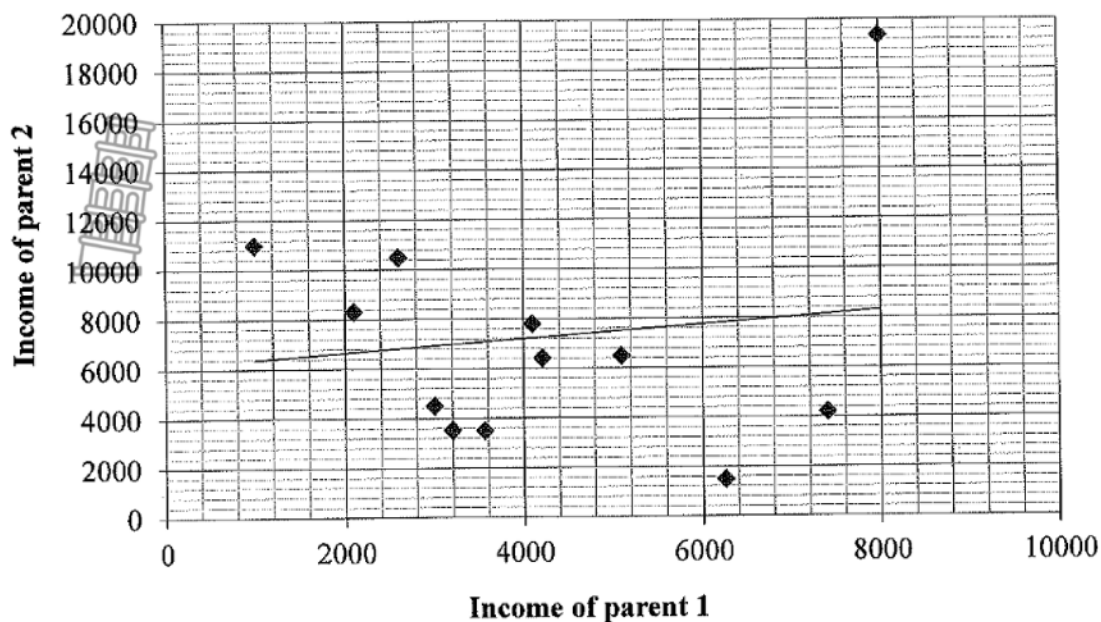
**QUESTION/VRAAG 1**

|     |   |   |
|-----|---|---|
| 1.1 | $\frac{87110}{12} = R 7259,17$  | ✓ R 7259,17<br>(2)  |
| 1.2 | SD = R4579,26<br>Above ONE standard deviation = mean + 1SD<br>$= R 7259,17 + R 4579,26$<br>$= R 11838,43$<br><br>Only ONE household | ✓ SD<br>✓ boundary<br><br>✓ answer<br>(3)                         |
| 1.3 | $y = a + bx$<br>$a = 6102,11$<br>$b = 0,27$<br>$y = 6102,11 + 0,27x$  | ✓ $a = 6102,11$<br>✓ $b = 0,27$<br>✓ $y = 6102,11 + 0,27x$<br>(3) |



1.4

## Scatter plot of income per household



✓✓ points correctly plotted

✓✓ regression line

(4)

1.5

The gradient of the line will become smaller, causing the data to be more symmetrical about the regression line, and there will be no outlier.

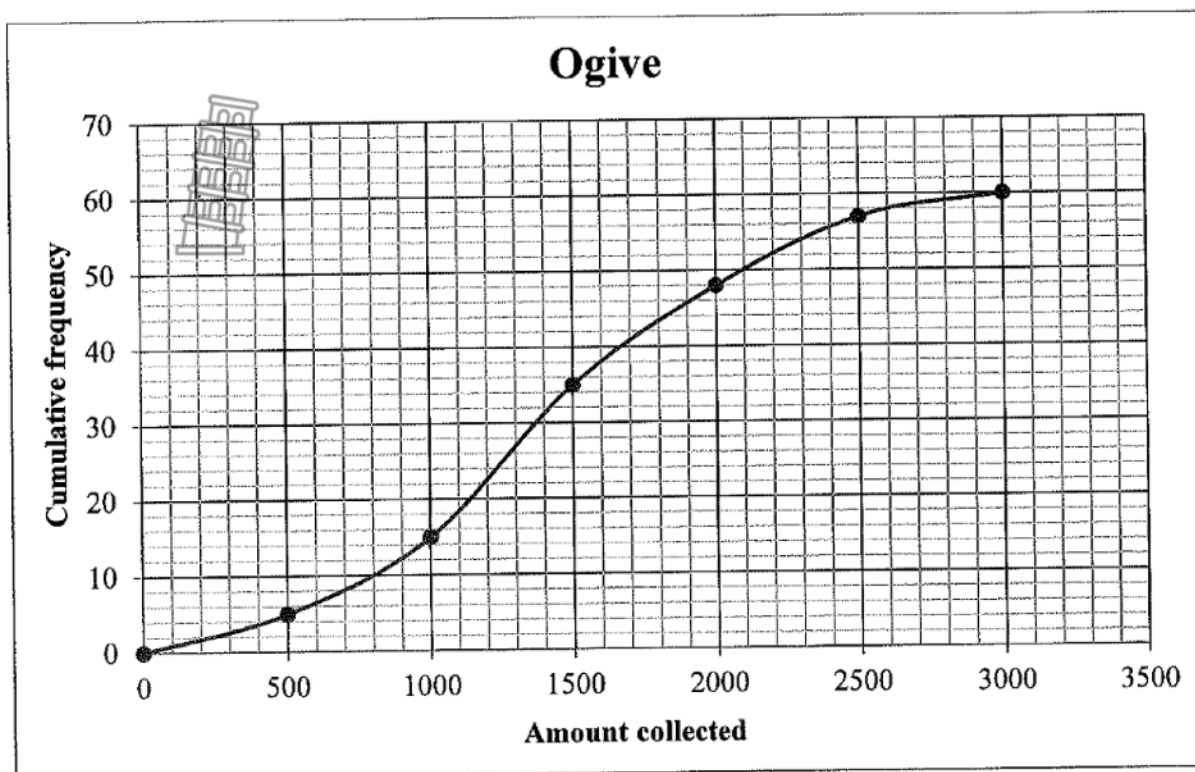
✓✓ answer

(2)

[14]

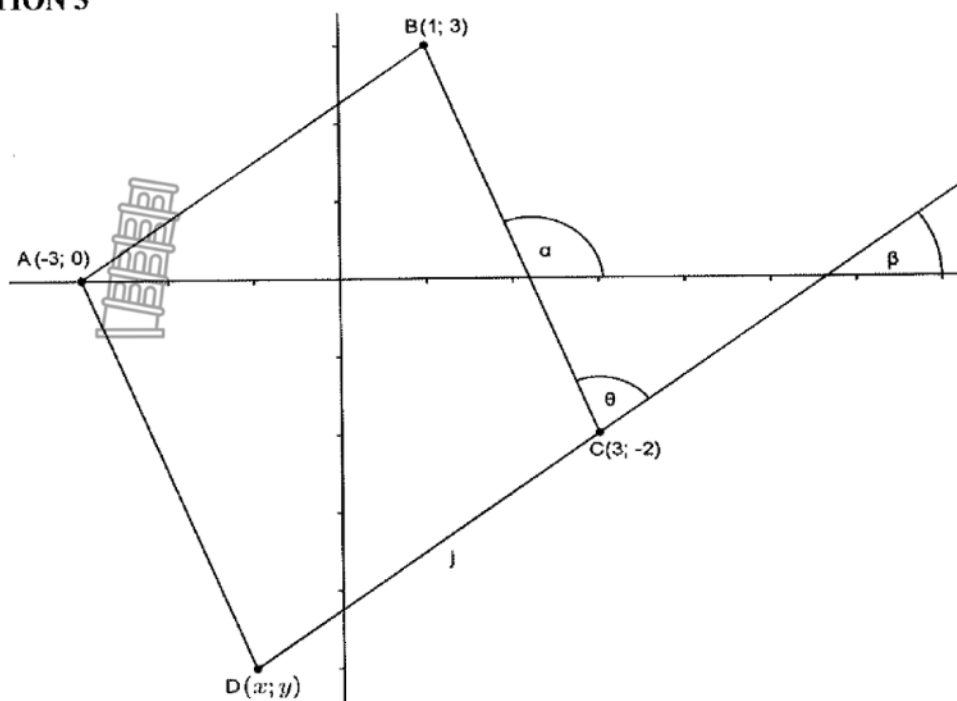


QUESTION/VRAAG 2



|     |  |  |
|-----|--|--|
| 2.1 | $1000 < x \leq 1500$   | ✓ answer<br>(1)                                |
| 2.2 | $60 - 15 = 45$ parents   | ✓ 15 and 60<br>✓ answer<br>(3)                 |
| 2.2 | $a = \text{lower quartile} = 1000$<br>$b = \text{median} = 1350$<br>$c = \text{upper quartile} = 1850$ | ✓ method<br>✓ Q1<br>✓ Q2<br>✓ Q3<br>(4)<br>[7] |
|     |  |  |
|     |  |  |

QUESTION 3



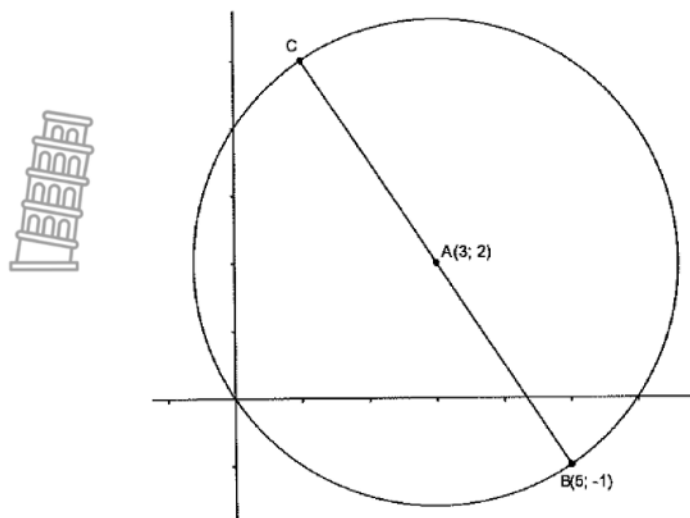
|     |   |  |
|-----|---|--|
| 3.1 | $D(-1; -5)$   | ✓✓ (2)   |
| 3.2 | $m_{AB} = \frac{3-0}{1-(-3)} = \frac{3}{4}$ $m_{BC} = \frac{3-(-2)}{1-3} = \frac{5}{-2}$ $\frac{3}{4} \times \frac{5}{-2} = \frac{15}{-8} \neq -1$ <p><math>\therefore</math> AB not perpendicular to BC, <math>\therefore</math> ABCD is not a rectangle</p> | $m_{AB}$ ✓<br>$m_{BC}$ ✓<br>$\neq -1$ ✓<br>Not rectangle ✓ (4) |
| 3.3 | $M_{AB} = \left(\frac{-3+1}{2}; \frac{0+3}{2}\right) = (-1; \frac{3}{2})$   | ✓✓ (2)   |
| 3.4 | $m_{AB} = \frac{3}{4}, \therefore m_{\perp} = -\frac{4}{3}$ $y - \frac{3}{2} = -\frac{4}{3}(x - (-1))$ $y = -\frac{4}{3}x - \frac{4}{3} + \frac{3}{2}$ $= -\frac{4}{3}x + \frac{1}{6}$  | $m_{\perp}$ ✓<br>Subst ✓<br>✓<br>(3)                           |
| 3.5 | $\tan \alpha = -\frac{5}{2}$ $\alpha = -68,198 \dots^{\circ} + 180^{\circ} = 111,80^{\circ}$ $\tan \beta = \frac{3}{4} \quad (AB \parallel CD)$ $\beta = 36,87^{\circ}$   | ✓<br>✓<br>✓  |

|     |   |  |
|-----|---|--|
|     | $\therefore \theta = 111,80^\circ - 36,87^\circ$<br>$= 74,93^\circ$ (ext $\angle$ of $\Delta$ )<br>$\hat{BCD} = 105,07^\circ$ (angles on straight line)   | ✓<br>✓<br>(5)  |
| 3.6 | $BC^2 = (1-3)^2 + (3-(-2))^2$<br>$= 4 + 25 = 29$<br>$BC = \sqrt{29}$<br>$CD^2 = (3-(-1))^2 + (-2-(-5))^2$<br>$= 16 + 9 = 25$<br>$CD = 5$<br>$\text{Area } \Delta BCD = \frac{1}{2} BC \cdot CD \cdot \sin \hat{BCD}$<br>$= \frac{1}{2} \cdot \sqrt{29} \cdot 5 \cdot \sin 105,07^\circ$<br>$= 13 \text{ units}^2$ | Subst in formula ✓<br>BC ✓<br>CD ✓<br>Subst in sine form<br>✓<br>✓ (5) |
|     |   | [21]   |



QUESTION 4

4.1



|       |   |                              |     |
|-------|---|------------------------------|-----|
| 4.1.1 | $r^2 = (5 - 3)^2 + (-1 - 2)^2$ $= 4 + 9 = 13$ $\therefore (x - 3)^2 + (y - 2)^2 = 13$   | ✓<br>✓<br>✓✓                 | (4) |
| 4.1.2 | $C = (1; 5)$ (symmetry)   | ✓✓                           | (2) |
| 4.1.3 | $m_{AC} = \frac{5-2}{1-3} = \frac{3}{-2}$<br>$m_{\text{tangent}} = \frac{2}{3}$<br>$y - 5 = \frac{2}{3}(x - 1)$ $y = \frac{2}{3}x - \frac{2}{3} + 5$ $= x + 4\frac{1}{3}$ | ✓<br><br>✓<br><br>✓<br><br>✓ | (4) |
| 4.1.4 | $r = \sqrt{13}$ and horizontal lines $\sqrt{13}$ from centre.<br>$\therefore y = 2 + \sqrt{13}$ and<br>$y = 2 - \sqrt{13}$  | ✓<br>✓                       | (2) |
| 4.1.5 | $(x - 3)^2 + (y - 2)^2 = (4 + \sqrt{13})^2$<br>Or $(x - 3)^2 + (y - 2)^2 = 57,84$   | ✓ centre<br>✓ radius         | (2) |
| 4.2   | $x^2 + y^2 + 4y + 3 = 0$ $x^2 + y^2 + 4y + 2^2 = -3 + 2^2$ $x^2 + (y + 2)^2 = 1$  | ✓                            |     |



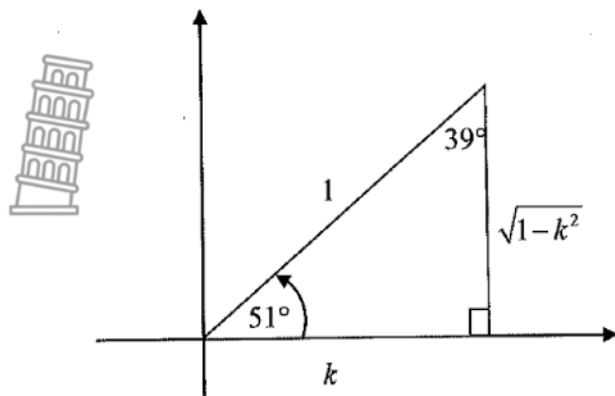
|  |  |  |
|--|--|--|
|  | <p>Centres: A: (3; 0) and B: (0; -2)</p> <p>Distance between centres <math>AB = \sqrt{(3 - 0)^2 + (2 - 0)^2} = \sqrt{13}</math><br/> <math>= 3,61</math></p> <p>Radii = 1 and 2</p> <p>Sum of radii = 3</p> <p>Sum of radii <math>\leq</math> Distance between centres</p> <p><math>\therefore</math> Circles do not intersect</p> | <p>✓</p> <p>✓</p> <p>✓</p> <p>✓</p> <p>✓ (6)</p> |
|  |  | [20]   |





QUESTION 5

5.1  $\cos 51^\circ = \frac{k}{1}$



|       |  |   |
|-------|--|---|
| 5.1.1 | $y^2 = 1^2 - k^2$ $y = \sqrt{1 - k^2}$<br>$\tan 219^\circ = \tan(180^\circ + 39^\circ)$ $= \tan 39^\circ$ $= \frac{k}{\sqrt{1 - k^2}}$   | ✓ Pythagoras<br><br>✓ $-\tan 39^\circ$<br>✓ answer<br>(3)                       |
| 5.1.2 | $\sin(-411^\circ) = \sin(-411^\circ + 360^\circ)$ $= \sin(-51^\circ)$ $= -\sin 51^\circ$ $= -\frac{\sqrt{1 - k^2}}{1}$   | ✓ reduction<br>✓ answer<br>(2)  |
| 5.1.3 | $\cos 9^\circ = \cos(60^\circ - 51^\circ)$ $= \cos 60^\circ \cos 51^\circ + \sin 60^\circ \sin 51^\circ$ $= \left(\frac{1}{2}\right)(k) + \left(\frac{\sqrt{3}}{2}\right)\left(\frac{\sqrt{1 - k^2}}{1}\right)$ $= \frac{1k}{2} + \frac{\sqrt{3(1 - k^2)}}{2}$ | ✓ compound angles<br>✓ expansion<br><br>✓ substitution<br>✓ substitution<br>(4) |



|     |  |   |
|-----|--|---|
| 5.2 | $\sin(45^\circ + x) \cdot \sin(45^\circ - x)$ $= (\sin 45 \cos x + \cos 45 \sin x)(\sin 45 \cos x - \cos 45 \sin x)$ $= \left( \frac{\sqrt{2}}{2} \cos x + \frac{\sqrt{2}}{2} \sin x \right) \left( \frac{\sqrt{2}}{2} \cos x - \frac{\sqrt{2}}{2} \sin x \right)$ $= \frac{1}{2} \cos^2 x - \frac{1}{2} \sin^2 x$ $= \frac{1}{2} \cos 2x$ | <ul style="list-style-type: none"> <li>✓ expansion</li> <li>✓ expansion</li> <li>✓ <math>\frac{\sqrt{2}}{2}</math></li> <li>✓ simplification</li> <li>✓ answer</li> </ul> <p style="text-align: right;">(5)</p>   |
| 5.3 | $\frac{\sin x + \sin 2x}{1 + \cos x + \cos 2x} = \tan x$ $LHS = \frac{\sin x + \sin 2x}{1 + \cos x + \cos 2x}$ $= \frac{\sin x + 2 \sin x \cos x}{1 + \cos x + 2 \cos^2 x - 1}$ $= \frac{\sin x + 2 \sin x \cos x}{\cos x + 2 \cos^2 x}$ $= \frac{\sin x(1 + 2 \cos x)}{\cos x(1 + 2 \cos x)}$ $= \tan x = RHS$                            | <ul style="list-style-type: none"> <li>✓ <math>2 \sin x \cos x</math></li> <li>✓ <math>2 \cos^2 x - 1</math></li> <li>✓ simplification of denominator</li> <li>✓ common factor</li> <li>✓ common factor</li> <li>✓ <math>\frac{\sin x}{\cos x} = \tan x</math></li> </ul> <p style="text-align: right;">(6)</p> |
| 5.4 | $\sin 15^\circ = \sin(45^\circ - 30^\circ)$ $= \sin 45 \cos 30 - \cos 45 \sin 30$ $= \left( \frac{\sqrt{2}}{2} \right) \left( \frac{\sqrt{3}}{2} \right) - \left( \frac{\sqrt{2}}{2} \right) \left( \frac{1}{2} \right)$ $= \frac{\sqrt{6} - \sqrt{2}}{4}$   | <ul style="list-style-type: none"> <li>✓ <math>\sin(45^\circ - 30^\circ)</math></li> <li>✓ expansion</li> <li>✓ substitution</li> <li>✓ simplification <math>\sqrt{6}</math></li> </ul> <p style="text-align: right;">(4)</p>   |

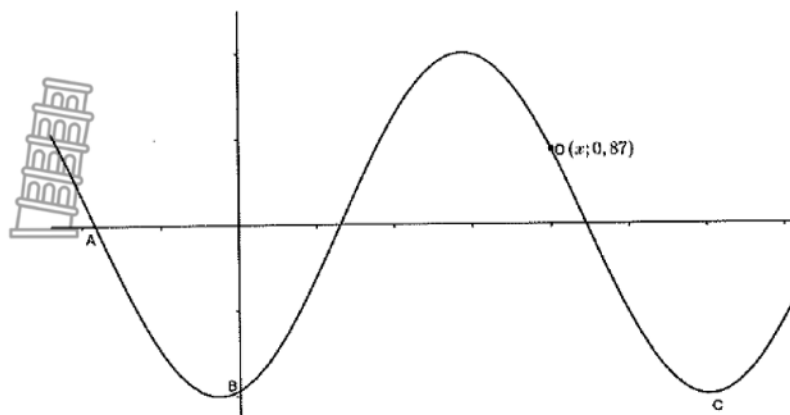


|     |   |   |
|-----|---|---|
| 5.5 | $\frac{(\sin x - \cos x)^2 - 1}{\sin^2 x - 1} = 2$ $\sin^2 x - 2\sin x \cos x + \cos^2 x - 1 = 2(\sin^2 x - 1)$ $\sin^2 x - 2\sin x \cos x + \cos^2 x - 1 = 2\sin^2 x - 2$ $-2\sin^2 x - 2\sin x \cos x + 2 = 0$ $-\sin^2 x - \sin x \cos x + 1 = 0$ $-\sin^2 x - \sin x \cos x + \sin^2 x + \cos^2 x = 0$ $\cos^2 x - \sin x \cos x = 0$ $\cos x(\cos x - \sin x) = 0$ $\cos x = 0 \quad \text{or} \quad \cos x - \sin x = 0$ $x = \pm 90^\circ + 360k \quad \cos x = \sin x$ $\tan x = 1$ $x = 45^\circ + 180k, k \in \mathbb{Z}$ | $\checkmark 2\sin^2 x - 2$<br><br>$\checkmark \sin^2 x + \cos^2 x$<br>$\checkmark$ standard form<br>$\checkmark$ common factor<br><br>$\checkmark x = \pm 90 + 360k \quad k \in \mathbb{Z}$<br><br>$\checkmark \tan x = 1$<br>$\checkmark x = 45^\circ + 180k$<br><br><div style="text-align: right;">(7)</div> |
|     |   | [31]  |



# QUESTION 6

The graph of  $f(x) = -2 \cos(x + 15^\circ)$  is given.

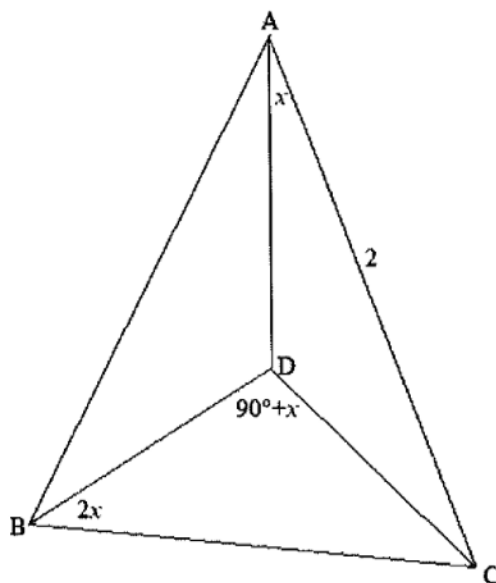


|       |  |                 |      |
|-------|--|-----------------|------|
| 6.1   | Amplitude = 2  | ✓               | (1)  |
| 6.2   | Period = $360^\circ$   | ✓               | (1)  |
| 6.3   | Range of $g(x)$ : $y \in [0; 4]$   | ✓✓              | (2)  |
| 6.4.1 | $\therefore A = (-105^\circ; 0)$   | ✓✓              | (2)  |
| 6.4.2 | $B = (0, -1,93)$   | ✓✓              | (2)  |
| 6.4.3 | $C = (165^\circ; -2)$  | ✓✓              | (2)  |
| 6.4.4 | $-2 \cos(x + 15^\circ) = 0,87$<br>$\cos(x + 15^\circ) = -0,435$<br>$x + 15^\circ = 115,785 \dots^\circ + 360k, k \in \mathbb{Z}$<br>$x = 100,79^\circ + 360k$<br>$\therefore D = (100,79^\circ; 0,87)$ | ✓<br><br>✓<br>✓ | (3)  |
|       |  |                 | [13] |



## QUESTION 7

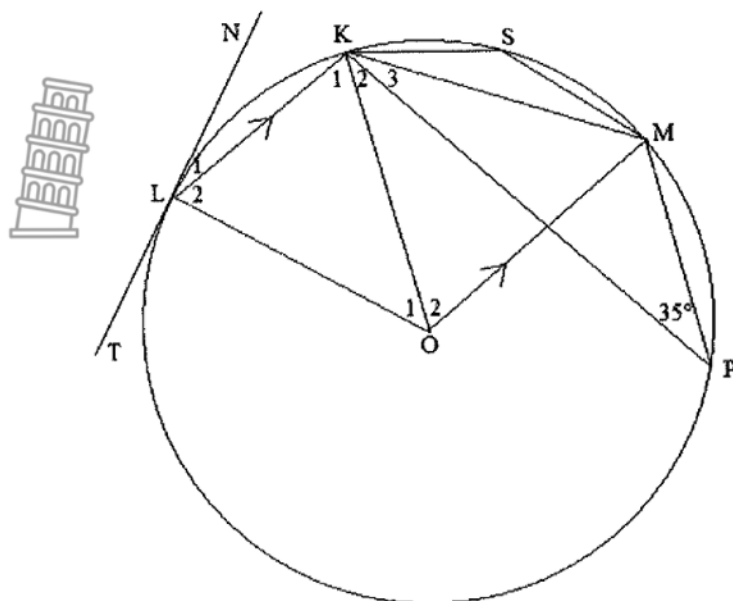
AD is a vertical pole and points B and C are in the same horizontal plane as D, the foot of the tower.  $\widehat{DAC} = x$ ,  $\widehat{BDC} = 2x$ ,  $\widehat{BDC} = 90^\circ + x$  and  $AC = 2$ .



|     |   |   |
|-----|---|---|
| 7.1 | $\sin x = \frac{CD}{2}$ $CD = 2 \sin x$ $\frac{BC}{\sin(90^\circ + x)} = \frac{CD}{\sin 2x}$ $\frac{BC}{\cos x} = \frac{2 \sin x}{2 \sin x \cos x}$ $BC = \frac{2 \sin x \cdot \cos x}{2 \sin x \cos x}$ $= 1$  | <p>✓</p> <p>✓</p> <p>Subst in Sin-rule ✓</p> <p>Cos x ✓</p> <p>2 sinx cosx ✓</p> <p>Simplification ✓</p> <p>(6)</p> |
| 7.2 | $\widehat{BCD} = 180^\circ - (90^\circ + x) - 2x$ $= 90^\circ - 3x$ <p>In <math>\triangle BCD</math>:</p> $\frac{BD}{\sin(90^\circ - 3x)} = \frac{1}{\sin(90^\circ + x)}$ $\frac{BD}{\cos 3x} = \frac{1}{\cos x}$ $\frac{\cos 3x}{\cos x} = 2 \cos 2x - 1.$ | <p>✓</p> <p>✓</p> <p>Subst in sine-form</p> <p>Co-functions ✓ (3)</p> <p>[9]</p>                                    |

**Question 8**

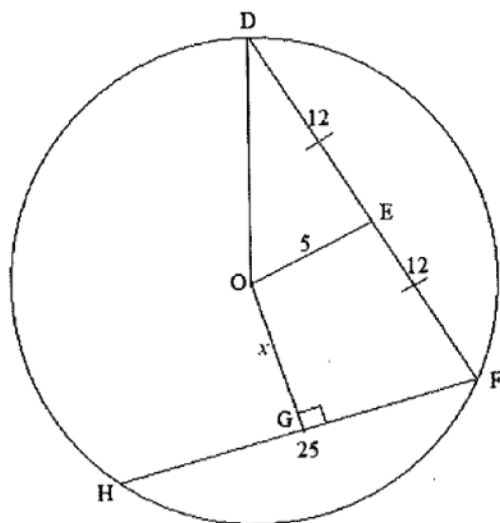
8.1 In the diagram, O is the centre of the circle.  $KL \parallel OM$ , NLT is a tangent to the circle at L.



|       |  |  |                                   |
|-------|--|--|-----------------------------------|
| 8.1.1 | $\hat{O}_2 = 70^\circ$   | $\angle$ at centre circle = $2 \times \angle$ at circumf                                   | S ✓ R ✓ (2)                       |
| 8.1.2 | $\hat{K}_1 = 70^\circ$<br>$\hat{L}_2 = 70^\circ$<br>$\hat{O}_1 = 40^\circ$ | alt. $\angle$ s, $KL \parallel MO$<br>$\angle$ s opp = radii<br>int $\angle$ s of $\Delta$ | S + R ✓<br>S + R ✓<br>S + R ✓ (3) |
| 8.1.3 | $\hat{L}_1 = 20^\circ$   | radius $\perp$ tangent   | S ✓ R ✓ (2)                       |
| 8.1.4 | $\hat{S} = 135^\circ$  | opp $\angle$ of cyclic quad  | S ✓ R ✓ (2)                       |



8.2



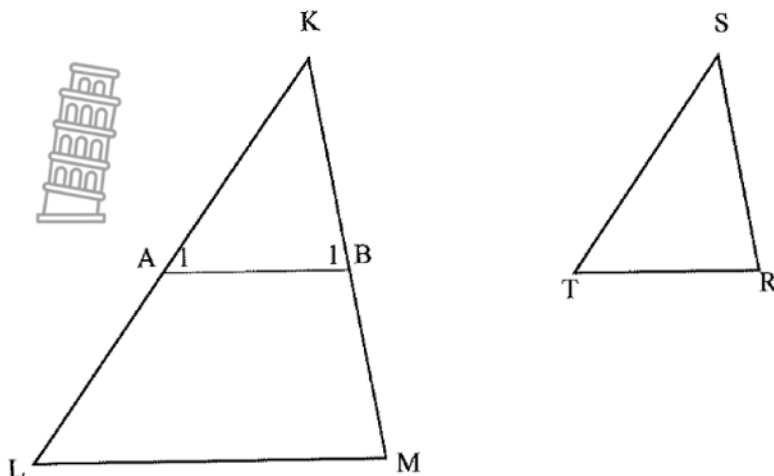
|       |  |   |                   |      |
|-------|--|---|-------------------|------|
| 8.2.1 | $\angle OED = 90^\circ$<br>$OD^2 = 12^2 + 5^2$<br>$= 169$<br>$OD = 13$ | Centre circle midpoint chord<br>Theorem of Pythagoras | S ✓ R ✓<br>✓<br>✓ | (4)  |
| 8.2.2 | $FG = 12,5$  | Centre circle $\perp$ chord                           | S ✓ R ✓           | (2)  |
|       |  |   |                   | [15] |





## QUESTION 9

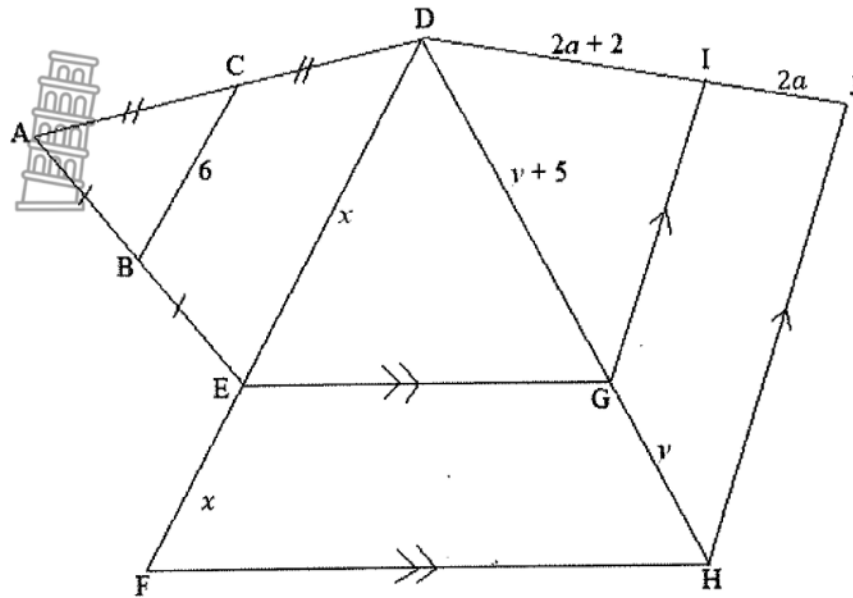
9.1 In  $\triangle KLM$  and  $\triangle STR$ ,  $\hat{K} = \hat{S}$ ,  $\hat{L} = \hat{T}$ ,  $\hat{M} = \hat{R}$ . Prove that  $\frac{ST}{KL} = \frac{SR}{KM}$ . (6)



|     |  |  |
|-----|--|--|
| 9.1 | <p>Construction</p> <p>In <math>\triangle KAB</math> and <math>\triangle STR</math>:</p> <p><math>AK = ST</math> construction</p> <p><math>KB = SR</math> construction</p> <p><math>\hat{K} = \hat{S}</math> given</p> <p><math>\therefore \triangle KAB \cong \triangle STR</math> SAS</p> <p><math>\therefore \hat{A}1 = \hat{T}</math></p> <p>But <math>\hat{T} = \hat{L}</math> given</p> <p><math>\therefore \hat{A}1 = \hat{L}</math></p> <p><math>\therefore AB \parallel LM</math> corresponding angles =</p> <p><math>\therefore \frac{KA}{KL} = \frac{KB}{KM}</math> line // one side of <math>\triangle</math></p> <p><math>\therefore \frac{ST}{KL} = \frac{SR}{KM}</math> <math>AK = ST</math> and <math>KB = SR</math></p> | <p>✓</p> <p>✓</p> <p>✓</p> <p>✓</p> <p>✓</p> <p>✓</p> <p>(6)</p> |
|-----|--|--|

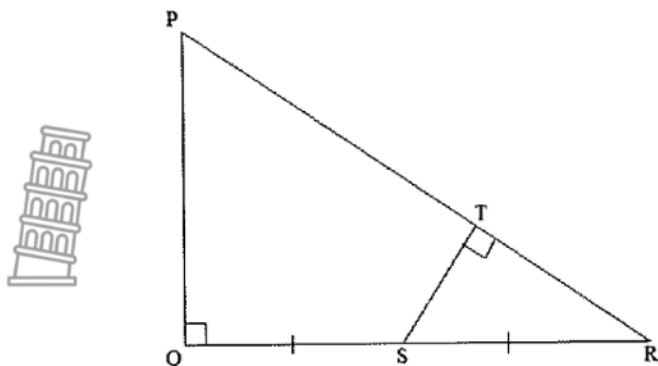


9.2 In the sketch  $EG \parallel FH$  and  $GI \parallel HJ$ .  $AB = BE$  and  $AC = CD$ .  $BC = 6$ ,  $DE = x$ ,  $EF = x - 3$ ,  $DG = y + 5$ ,  $GH = y$ ,  $DI = 2a + 2$  and  $IJ = 2a - 3$ .



|     |  |                                 |                  |      |
|-----|--|---------------------------------|------------------|------|
| 9.1 | $x = 12$   | midpt theorem                   | S ✓ R ✓          | (2)  |
| 9.2 | $\frac{x}{x-3} = \frac{y+5}{y}$ $\frac{12}{9} = \frac{y+5}{y}$ $12y = 9y + 45$ $3y = 45$ $y = 15$                          | line // to one side of $\Delta$ | S ✓ R ✓<br><br>✓ | (3)  |
| 9.3 | $\frac{2a+2}{2a-3} = \frac{y+5}{y}$ $\frac{2a+2}{2a-3} = \frac{20}{15} = \frac{4}{3}$ $6a + 6 = 8a - 12$ $2a = 18$ $a = 9$ | line // to one side of $\Delta$ | S ✓ R ✓<br><br>✓ | (3)  |
|     |  |                                 |                  | [14] |

## QUESTION 10



|      |   |   |
|------|---|---|
| 10.1 | <p>In <math>\triangle PQR</math> and <math>\triangle STR</math></p> <p><math>\hat{Q} = \hat{T}</math> <math>90^\circ</math> given</p> <p><math>\hat{R} = \hat{R}</math> common <math>\angle</math></p> <p><math>\therefore \hat{P} = \hat{S}</math> int <math>\angle</math>s of <math>\Delta</math></p> <p><math>\triangle PQR \parallel \triangle STR</math> A A A</p> | <p>S + R ✓</p> <p>S + R ✓</p> <p>S + R ✓</p> <p>R ✓ (4)</p> |
| 10.2 | <p><math>\frac{PQ}{ST} = \frac{RQ}{RT} = \frac{PR}{RS}</math> similarity</p> <p><math>\therefore PR \cdot RT = RS \cdot RQ</math></p> <p>but <math>RS = QS</math></p> <p><math>\therefore PR \cdot RT = QS \cdot RQ</math></p>  | <p>✓</p> <p>✓ (2)</p>                                       |
|      |   | [10]  |

TOTAL: 150



## MATHEMATICS P2 JUNE 2021 GRID

|     |                    | 1 | 2 | 3 | 4 | TOTAL |
|-----|--------------------|---|---|---|---|-------|
| 1.1 | median             |   | 2 |   |   |       |
| 1.2 | mean               | 2 |   |   |   |       |
| 1.3 | standard deviation |   | 3 |   |   |       |
| 1.4 | regression line    | 3 |   |   |   |       |
| 1.5 | scatter plot       |   | 4 |   |   |       |
| 1.6 | interpret          |   |   |   | 2 |       |

|     |                 |   |   |   |  |  |
|-----|-----------------|---|---|---|--|--|
| 2.1 | modal class     | 1 |   |   |  |  |
| 2.2 | interpret ogive |   | 3 |   |  |  |
| 2.3 | interpret ogive |   |   | 4 |  |  |

|     |                  |   |   |   |  |  |
|-----|------------------|---|---|---|--|--|
| 3.1 | coordinates      | 2 |   |   |  |  |
| 3.2 | Rectangle        |   | 4 |   |  |  |
| 3.3 | midpoint         |   |   | 1 |  |  |
| 3.4 | equation of line |   |   | 2 |  |  |
| 3.5 | size of angle    |   |   | 3 |  |  |
| 3.6 | area triangle    |   | 3 |   |  |  |
|     |                  |   |   |   |  |  |
|     |                  |   |   |   |  |  |
|     |                  |   |   |   |  |  |

|       |                     |   |   |   |  |  |
|-------|---------------------|---|---|---|--|--|
| 4.1.1 | equation circle     |   | 4 |   |  |  |
| 4.1.2 | coordinates         | 2 |   |   |  |  |
| 4.1.3 | equation tangent    |   | 4 |   |  |  |
| 4.1.4 | horizontal tangents |   |   | 2 |  |  |
| 4.1.5 | new circle          |   |   | 2 |  |  |
| 4.2   | circles intersect   |   |   | 6 |  |  |

|       |                    |   |   |   |   |   |
|-------|--------------------|---|---|---|---|---|
| 5.1.1 | reduction          | 3 |   |   |   |   |
| 5.1.2 | reduction          | 2 |   |   |   |   |
| 5.1.3 | compound angle     |   | 4 |   |   |   |
| 5.2   | compound expansion |   |   | 5 |   |   |
| 5.3   | identities         |   |   | 6 |   |   |
| 5.4   | identities         |   |   | 4 |   |   |
| 5.5   | general solution   |   |   |   | 7 |   |
|       |                    |   |   |   |   |   |
| 6.1   | amplitude          | 1 |   |   |   |   |
| 6.2   | period             | 1 |   |   |   | 4 |

|       |               |  |   |   |   |    |
|-------|---------------|--|---|---|---|----|
| 6.3   | range         |  | 2 |   |   |    |
| 6.4.1 | x-intercept   |  |   |   |   |    |
| 6.4.2 | y-intercept   |  | 2 |   |   |    |
| 6.4.3 | turning point |  | 2 |   |   |    |
| 6.4.4 | x-coordinate  |  |   | 3 |   |    |
| 7.1   | show length   |  |   |   | 5 | 12 |

|       |                     |  |   |   |  |  |
|-------|---------------------|--|---|---|--|--|
| 7.2   | show that           |  |   |   |  |  |
| 8.1.1 | angle at centre     |  | 3 |   |  |  |
| 8.1.2 | int angles triangle |  |   | 3 |  |  |

|              |                                   |           |           |           |           |           |
|--------------|-----------------------------------|-----------|-----------|-----------|-----------|-----------|
| 8.1.3        | tan perp radius                   | 3         |           |           |           |           |
| 8.1.4        | opp angles cycliq                 |           |           | 2         |           | 11        |
| 8.2.1        | Pyth                              |           |           |           |           |           |
| 8.2.2        | centre circle perp chord          | 5         |           |           |           |           |
| 9.2.1        | cyclic quad                       |           | 4         |           |           |           |
| 9.2.2        | congruency                        |           | 3         |           |           |           |
| 9.2.3        | angle at centre                   |           |           | 5         |           |           |
| 9.2.4        | same segment                      |           |           | 5         |           | 22        |
| 10.1         | properties of parm                | 1         |           |           |           |           |
| 10.2         | one line // to 3 line in triangle |           | 3         |           |           |           |
| 10.3         | area rule                         |           | 2         |           |           | 6         |
| 11.1         | similarity                        | 3         |           |           |           |           |
| 11.2         | ratio                             |           | 3         |           |           |           |
| 11.3         | ratio                             |           |           | 5         |           | 11        |
| <b>TOTAL</b> |                                   | <b>29</b> | <b>55</b> | <b>58</b> | <b>14</b> | <b>66</b> |

