



# **PROVINCIAL EXAMINATION**

## **NOVEMBER 2022**

### **GRADE 11**

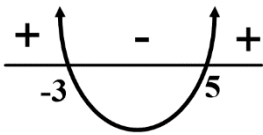
### **MARKING GUIDELINES**

<b>MATHEMATICS (PAPER 1)</b>
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**19 pages**

## QUESTION 1

1.1	1.1.1	<p>When <math>x = 2</math> and when <math>x = 3</math></p> $\sqrt{3-x} \qquad \qquad \qquad \sqrt{3-3}$ $\sqrt{3-2} \qquad \qquad \qquad \sqrt{0}$ <p style="text-align: center;"><i>and</i></p> $\sqrt{1} \qquad \qquad \qquad = 0$ $= 1$ $\therefore x = 2 \text{ or } x = 3$	✓ ✓ answers	(2)
	1.1.2	$\sqrt{3-x} = 2x - 3$ $\therefore 3 - x \geq 0 \text{ and } 2x - 3 \geq 0$ $\therefore -x \geq -3 \text{ and } 2x \geq 3$ $\therefore x \leq 3 \text{ and } x \geq \frac{3}{2}$ $\therefore \frac{3}{2} \leq x \leq 3$ <p><b>NOTE:</b> Answer can be written as separate inequalities.</p> <p style="text-align: center;"><b>OR</b></p> <p><b>NOTE:</b> If the candidates solve the equation, the answers are: <math>x = \frac{3}{4}</math> or <math>x = 2</math>, the answer of <math>x = \frac{3}{4}</math> must be rejected to obtain <math>\frac{3}{3}</math>, but if not rejected, award <math>\frac{2}{3}</math>.</p>	<p>✓ setting up correct inequalities</p> <p>✓ ✓ answers</p>	(3)
1.2		$(3a - 8)(2b + 7) = 0$ $\therefore 3a - 8 = 0 \text{ or } 2b + 7 = 0$ $\therefore a = \frac{8}{3}$ $\therefore b = -\frac{7}{2}$	<p>✓ value of <math>a</math></p> <p>✓ value of <math>b</math></p>	(2)

1.3	1.3.1	$4x^2 - 20x + 1 = 0$  $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$  $x = \frac{-(-20) \pm \sqrt{(-20)^2 - 4(4)(1)}}{2(4)}$  $x = \frac{20 \pm \sqrt{384}}{8}$  $\therefore x = 4,95 \text{ or } x = 0,05$  <b>NOTE:</b> Penalise one mark for incorrect rounding-off in this question ONLY.	✓ substitution         ✓✓ answers	(3)
	1.3.2	$(x+1)(x-3) > 12$  $x^2 - 2x - 3 > 12$  $x^2 - 2x - 15 > 0$  $(x-5)(x+3) > 0$    $\therefore x > 5 \text{ or } x < -3$	✓ standard form  ✓ factors       ✓✓ answers	(4)
	1.3.3	$x - \sqrt{5+x} = 7$  $x - 7 = \sqrt{5+x}$  $(x-7)^2 = (\sqrt{5+x})^2$  $x^2 - 14x + 49 = 5 + x$  $x^2 - 15x + 44 = 0$  $(x-4)(x-11) = 11$  $x = 11 \text{ or } x \neq 4$	✓ squaring both sides  ✓ simplification  ✓ standard form  ✓ factors  ✓ answers with rejection	(5)

1.4	1.4.1	$x = 3$ and $y = a$ $\therefore x - y = 1$ $\therefore 3 - a = 1$ $\therefore a = 2$ <i>but</i> $x^2 - 3xy + by^2 = -5$ $\therefore 3^2 - 3(3)(2) + b(2)^2 = -5$ $\therefore 9 - 18 + 4b = -5$ $\therefore 4b = 4$ $\therefore b = 1$	✓ value of $a$ ✓ substitute for $x$ and $y$  ✓ simplification ✓ value of $b$	(4)
	1.4.2	$x - y = 1$ $\therefore x = y + 1 \dots\dots(1)$ $x^2 - 3xy + y^2 = -5 \dots\dots(2)$ $\therefore (y + 1)^2 - 3y(y + 1) + y^2 = -5$ $\therefore y^2 + 2y + 1 - 3y^2 - 3y + y^2 = -5$ $\therefore -y^2 - y + 6 = 0$ $\therefore y^2 + y - 6 = 0$ $\therefore (y + 3)(y - 2) = 0$ $\therefore y = -3$ or $y = 2$ $\therefore x = -2$ or $x = 3$ The other solution: $(-2; -3)$ <b>NOTE:</b> Candidates do not have to write the answer in coordinate form.	✓ $x$ as subject  ✓ substitute into (2)  ✓ standard form ✓ factors  ✓ $y$ -values ✓ $x$ -values	(6)

1.5	1.5.1	$(p + 1)x^2 + 2px + (p + 2) = 0$ $\Delta = b^2 - 4ac$ $\Delta = (2p)^2 - 4(p + 1)(p + 2)$ $\Delta = 4p^2 - 4p^2 - 12p - 8$ $\Delta = -12p - 8$ For equal roots, $\Delta = 0$ $-12p - 8 = 0$ $\therefore p = -\frac{8}{12}$ $\therefore p = -\frac{2}{3}$	✓ substitution for $\Delta$  ✓ expression for $\Delta$  ✓ condition for $\Delta$   ✓ answer	(4)
	1.5.2	$\Delta > 0$ $\therefore -12p - 8 > 0$ $\therefore p < -\frac{2}{3}$	✓ condition of $\Delta$   ✓ answer	(2)
				<b>[35]</b>

## QUESTION 2

2.1	2.1.1	$\left(\frac{1}{3^{n-1}} \cdot \frac{1}{3^{n+1}}\right)^{\frac{1}{n}}$ $= (3^{-n+1} \cdot 3^{-n-1})^{\frac{1}{n}}$ $= (3^{-2n})^{\frac{1}{n}}$ $= 3^{-2}$ $= \frac{1}{9}$ <p><b>NOTE:</b> Any other valid method.</p>	<p>✓ simplification</p> <p>✓ simplification</p> <p>✓ answer</p>	(3)
	2.1.2	$-\sqrt[3]{27^2} - \frac{2}{8^{-\frac{2}{3}}} + \frac{\sqrt[5]{2}}{4^{-\frac{2}{5}}}$ $= [(3^3)^2]^{\frac{1}{3}} - \frac{2}{(2^3)^{-\frac{2}{3}}} + \frac{2^{\frac{1}{5}}}{(2^2)^{-\frac{2}{5}}}$ $= 3^2 - \frac{2}{2^{-2}} + \frac{2^{\frac{1}{5}}}{2^{-\frac{4}{5}}}$ $= 9 - 2^3 + 2^1$ $= 3$ <p><b>NOTE:</b> Any other valid method.</p>	<p>✓ simplification</p> <p>✓ simplification</p> <p>✓ simplification</p> <p>✓ answer</p>	(4)

2.2	$3^{2-x} + 8 = 3^x$ $3^2 \cdot 3^{-x} + 8 = 3^x$ $\frac{9}{3^x} + 8 = 3^x$ $9 + 8 \cdot 3^x = 3^{2x}$ $3^{2x} + 8 \cdot 3^x - 9 = 0$ $(3^x - 9)(3^x + 1) = 0$ $3^x = 9 \text{ or } 3^x = -1$ $3^x = 3^2 \text{ or } NA$ $\therefore x = 2$ <b>NOTE:</b> Any other valid method.	✓ simplification  ✓ standard form ✓ factors  ✓ answer with rejection	(4)
			[11]

## QUESTION 3

3.1	1 ; 2 ; 5 ; 10 +1 +3 +5 +2 +2 $2a = 2$ $3a + b = 1$ $a + b + c = 1$ $a = 1$ $3(1) + b = 1$ $1 - 2 + c = 1$ $b = -2$ $c = 2$ $\therefore T_n = n^2 - 2n + 2$ <b>NOTE:</b> No penalty if not written as an equation.	$2^{nd}$ difference ✓ value of $a$ ✓ value of $b$ ✓ value of $c$	(4)
3.2	$T_{50} = 50^2 - 2(50) + 2$ $T_{50} = 2402$	✓ substitution ✓ answer	(2)
3.3	ROW 11	✓✓ answer	(2)

3.4	$1 ; 3 ; 5 ; 7$ $+2 \quad +2 \quad +2$ $T_n = 2n - 1$ $241 = 2n - 1$ $n = 121$	✓ correct equation ✓ $T_n = 241$ ✓ answer	(3)
			<b>[11]</b>

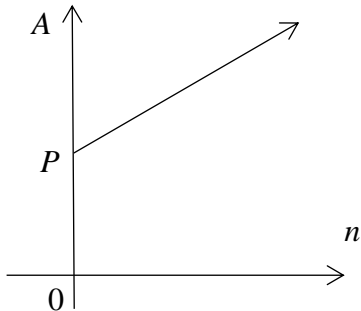
**QUESTION 4**

4.1	$4 \quad ; \quad 9 \quad ; \quad x \quad ; \quad 37 \dots$ $\quad \swarrow \quad \quad \swarrow \quad \quad \swarrow$ $5 \quad ; \quad x-9 \quad ; \quad 37-x$ $\quad \swarrow \quad \quad \swarrow$ $x-9-5 \quad ; \quad 37-x-(x-9)$ $x-14 \quad ; \quad 46-2x$ $x-14 = 46-2x$ $\therefore 3x = 60$ $\therefore x = 20$	✓ 1 <sup>st</sup> differences ✓ 2 <sup>nd</sup> differences  ✓ equating  ✓ answer	(4)
4.2	$5 ; 11 ; 17 ; \dots$ (first differences) $T_n = 6n - 1$ $599 = 6n - 1$ $600 = 6n$ $n = 100$ $\therefore$ Between 100 <sup>th</sup> and 101 <sup>th</sup> terms	✓ correct equation ✓ equating  ✓ value of $n$  ✓ conclusion	(4)

4.3	4.3.1	$\begin{array}{ccccc} 4 & ; & 9 & ; & 20 & ; & 37 \\ & & 5 & & 11 & & 17 \\ & & & & 6 & & 6 \end{array}$ $2a = 6$ $a = 3$ $\therefore T_n = 3n^2 + bn + c$ <p>Since the <math>a</math>-value is positive, <math>T_n</math> has a MINIMUM value.</p>	<p>✓ <math>2^{nd}</math> difference</p> <p>✓ value of <math>a</math></p> <p>✓ conclusion</p>	(3)
	4.3.2	$y = 3n^2 - 4n + 5$ $\therefore x = \frac{-(-4)}{2(3)}$ $\therefore x = \frac{4}{6}$ $\therefore x = \frac{2}{3}$ $\therefore f\left(\frac{2}{3}\right) = \frac{11}{3}$ $\therefore \text{range: } y \geq \frac{11}{3}$ <p style="text-align: center;"><b>OR</b></p> $y \in \left[\frac{11}{3}; \infty\right)$ <p><b>NOTE:</b> Correct brackets must be used to obtain the answer mark in option 2. This is a <b>theoretical</b> solution as it is understood that a number pattern is composed of terms which are indicated as natural numbers.</p>	<p>✓ value of <math>x</math></p> <p>✓ value of <math>f\left(\frac{2}{3}\right)</math></p> <p>✓ answer</p>	(3)



5.2	$A = P(1 + in)$ $\therefore 7\,500 = 6\,800(1 + 0,075n)$ $\therefore \frac{7\,500}{6\,800} - 1 = 0,075n$ $\therefore 0,075n = 0,10$ $\therefore n = 1,333 \text{ yrs}$ $\therefore n = 1,333(12)$ $\therefore n = 15,996$ $\therefore n \approx 16 \text{ mnths}$ <b>NOTE:</b> The answer mark is for 16 months.		✓ substitution into correct formula          ✓ value of $n$          ✓ answer	(3)
5.3	Compounded semiannually for 6 years. $\therefore n = 12$ $\therefore i = \frac{0,05}{2} = 0,025$ $A = P(1 + i)^n$ $A = 5\,000(1 + 0,025)^{12}$ $\therefore A = R6\,724,44$		✓ value of $n$ and $i$          ✓ substitution into correct formula ✓ answer	(3)
5.4	5.4.1	$A = P(1 + in)$ $A = P + Pin$ $\therefore$ linear function	✓ answer	(1)

5.4.2	$m = Pi$ $P > 0$ $i > 0$  $\therefore m > 0$		$\checkmark m > 0$ $\checkmark$ shape ( $c > 0$ )	(2)
5.4.3	$n = 0$ : $A = P + Pi(0)$  $\therefore A = P$  $n = 1$ : $A = P + Pi(1)$ $A = P + Pi$  $\therefore$ an INCREASE in $Pi$  <b>NOTE:</b> Answer only, full marks.		$\checkmark$ answer	(1)
				<b>[14]</b>

## QUESTION 6

6.1	$x = 2$ $y = 1$	✓ answer ✓ answer	(2)
6.2	$y = -1$	✓ answer	(1)
6.3		✓ shape of $f$ ✓ intercepts of $f$ ✓ shape of $g$ ✓ intercept of $g$	(4)
6.4	$x \in \mathbb{R}; x \neq 2$ <i>or</i> $x \in (-\infty; 2) \text{ or } (2; \infty)$ <b>NOTE:</b> Must state both conditions in option 1.	✓ answer	(1)
6.5	$y > -1$ <i>or</i> $y \in (-1; \infty)$	✓ answer	(1)
6.6	Point of intersection of asymptotes: $(2; 1)$ $y - y_1 = m(x - x_1)$ $y - 1 = -1(x - 2)$ $y = -x + 3$	✓ substitute $m$ and pt $(2; -1)$ ✓ answer	(2)
6.7	2 units to the right and 1 unit upwards	✓ units right ✓ units up	(2)

6.8	$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ $d = \sqrt{(2 - 0)^2 + (1 - 0)^2} \dots\dots (0;0)(2;1)$ $d = \sqrt{5}$ $d = 2,24$ <b>NOTE:</b> Answer only, full marks. No penalty for rounding-off incorrectly.	✓ correct substitution   ✓ answer	(2)
6.9	(3 ; 0)	✓ x-value ✓ y-value	(2)
6.10	$x \in (-\infty; 2)$ or $x < 2$	✓ answer	(1)
			<b>[18]</b>

**QUESTION 7**

7.1	$y = a(x - x_1)(x - x_2)$ $4 = a(0 - 1)(0 - 3)$ $4 = 3a$ $\therefore a = \frac{4}{3}$ $y = \frac{4}{3}(x - 1)(x - 3)$ $y = \frac{4}{3}(x^2 - 4x + 3)$ $y = \frac{4}{3}x^2 - \frac{16}{3}x + 4$	✓ substitute roots and point (0 ; 4)   ✓ value for $a$   ✓ answer	(3)
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7.2	$f(x) = \frac{4}{3}x^2 - \frac{16}{3}x + 4$ $x = \frac{-b}{2a}$ $x = \frac{-(-\frac{16}{3})}{2(\frac{4}{3})}$ $\therefore x = 2$ $\therefore f(2) = \frac{4}{3}(2)^2 - \frac{16}{3}(2) + 4$ $\therefore f(2) = -\frac{4}{3}$ $\therefore D(2; -\frac{4}{3})$ <p><b>NOTE:</b> Answer does not have to be in coordinate form.</p>	<p>✓ substitution into correct formula</p> <p>✓ x-value</p> <p>✓ y-value</p>	(3)
7.3	$m_g = \frac{0-4}{-8-0} \dots\dots (0;4)(-8;0)$ $\therefore m_g = \frac{1}{2}$ $\therefore m_p = -2$ $\therefore -\frac{4}{3} = -2(2) + c \dots\dots D(2; -\frac{4}{3})$ $\therefore c = 4 - \frac{4}{3}$ $\therefore c = \frac{8}{3}$ $\therefore p(x) = -2x + \frac{8}{3}$ <p><b>NOTE:</b> Answer does not have to be an equation.</p>	<p>✓ substitute correctly into gradient formula</p> <p>✓ value of <math>m_g</math></p> <p>✓ value of <math>m_p</math></p> <p>✓ substitute <math>m</math> and point D</p> <p>✓ value of <math>c</math></p>	(5)

7.4	$m = \tan \theta$  $\frac{1}{2} = \tan \theta$  $\therefore \theta = 26,57^\circ$		$\checkmark \tan \theta = \frac{1}{2}$  $\checkmark$ answer	(2)
7.5	$\frac{4}{3}x^2 - \frac{16}{3}x + 4 = \frac{1}{2}x + 4$  $\frac{4}{3}x^2 - \frac{35}{6}x = 0$  $x\left(\frac{4}{3}x - \frac{35}{6}\right) = 0$  $x = 0 \text{ of } x = \frac{35}{8}$  $y = \frac{1}{2}\left(\frac{35}{8}\right) + 4$  $y = \frac{99}{16}$  $K\left(\frac{35}{8}; \frac{99}{16}\right)$  <b>NOTE:</b> Answer does not need to be in coordinate form.		$\checkmark$ equating           $\checkmark$ factors           $\checkmark$ x-answers           $\checkmark$ y-answer from correct selection of x-value	(4)
7.6	7.6.1	$1 < x < 3$  <b>NOTE:</b> Can be written as separate inequalities.	$\checkmark$ answer	(1)
	7.6.2	$x \in (-8 ; 1] \text{ or } [3 ; \infty)$  <b>NOTE:</b> Penalise 1 mark if answer is not with correct brackets.	$\checkmark$ answer $\checkmark$ answer	(2)

7.7	$TP(2; -\frac{4}{3})$ from Q. 7.2  $\therefore f(x) = \frac{4}{3}(x-2)^2 - \frac{4}{3}$  $\therefore h(x) = \frac{4}{3}(x-4)^2 - \frac{13}{3}$		✓ equation of $f$  ✓ equation of $h$	(2)
7.8	7.8.1	$j(x) = ax - 8$  $\therefore 0 = -4a - 8 \dots pt(-4; 0)$  $\therefore 4a = -8$  $\therefore a = -2$	✓ substitution    ✓ answer	(2)
	7.8.2	The graph of $g$ to $j$ is a $90^\circ$ anticlockwise rotation about the origin.  <b>NOTE:</b> Accept, graphs are perpendicular and if $g$ is shifted anti-clockwise by $90^\circ$ , $j$ is obtained.	✓ answer	(1)
				<b>[25]</b>

**QUESTION 8**

8.1	Total = $13 + 7 + 24 + 3$  Total = 47		✓ answer	(1)
8.2	8.2.1	$P(M) = \frac{13+7}{47}$  $P(M) = \frac{20}{47} \dots or \dots 0,43$	✓ answer	(1)
	8.2.2	$P(M \text{ and } S) = \frac{7}{47} \text{ or } 0,15$	✓ answer	(1)
	8.2.3	$P(\text{not } M \text{ or } S) = \frac{3}{47} \text{ or } 0,06$	✓ answer	(1)

	8.2.4	$P(M \text{ or } S) = \frac{13 + 7 + 24}{47}$ $P(M \text{ or } S) = \frac{44}{47} \text{ or } 0,94$ <p style="text-align: center;"><b>OR</b></p> $P(M \text{ or } S) = P(M) + P(S) - P(M \text{ and } S)$ $= \frac{20}{47} + \frac{31}{47} - \frac{7}{47}$ $P(M \text{ or } S) = \frac{44}{47} \text{ or } 0,94$	✓ method  ✓ answer   ✓ method  ✓ answer	(2)
	8.2.5	$P(M \text{ or only } S) = \frac{13 + 24}{47}$ $P(M \text{ or only } S) = \frac{37}{47} \text{ or } 0,79$ <p><b>NOTE:</b> Answer only, full marks.</p>	✓ method  ✓ answer	(2)
8.3	8.3.1	$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$ $= 0,95 + 0,98 - 0,94$ $P(A \text{ or } B) = 0,99$ <p><b>NOTE:</b> Answer only, full marks.</p>	✓ correct substitution  ✓ answer	(2)
	8.3.2	$P(\text{Not Detected}) = 1 - 0,99$ $P(\text{Not Detected}) = 0,01$ <p><b>NOTE:</b> Answer only, full marks.</p>	✓ answer	(1)
				<b>[11]</b>

## QUESTION 9

9.1	9.1.1	NO. The survey was done on ONE day of the month and only in the morning.  <b>NOTE:</b> Answer must be NO.	✓ NO ✓ reasonable motivation	(2)
	9.1.2	The survey should be done:  <ul style="list-style-type: none"> <li>At different TIMES of the day.</li> <li>On different DAYS of the month, especially at the end of the month when most people do shopping.</li> </ul> <b>NOTE:</b> Any other valid reason.	✓ answer	(1)
9.2		$P(\text{black}) = \frac{26}{52} \times \frac{25}{51} \times \frac{24}{50}$ $\therefore P(\text{black}) = \frac{2}{17} \quad \text{or} \quad 0,118$ $P(\text{red}) = \frac{26}{52} \times \frac{25}{51} \times \frac{24}{50}$ $\therefore P(\text{red}) = \frac{2}{17} \quad \text{or} \quad 0,118$ $\therefore P(3 \text{ black or } 3 \text{ red}) = 0,118 + 0,118$ $\therefore P(3 \text{ black or } 3 \text{ red}) = 0,236 \quad \text{or} \quad \frac{59}{250}$	$\checkmark \frac{26}{52} \times \frac{25}{51} \times \frac{24}{50}$ $\checkmark \text{ answer } P(\text{black})$ $\checkmark \text{ answer } P(\text{red})$ $\checkmark \text{ method (+)}$ $\checkmark \text{ answer } P(3 \text{ black or } 3 \text{ red})$	(5)
				[8]
<b>TOTAL:</b>				<b>150</b>